

Collateral Demand in Wholesale Funding Markets

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ECB - Money Market Conference 2024

Views are solely those of the authors and not the Bank of England.

Repo Markets: How they work

Repurchase agreements (repo):

- ▶ Borrower sells asset at t & promises to buy it back at $t + 1$.
- ▶ Collateralized lending.
- ▶ Lender temporarily owns asset.

Repo serves two functions:

1. Funding demand: Acquiring funding cheaply.
→ Collateral valued only as insurance.
2. Collateral demand: Acquiring assets temporarily.
→ Usage of collateral valuable, eg to short.

Repo Markets: Why they matter

Important:

- ▶ Key wholesale funding market → financial stability.
- ▶ Necessary input to a shorting trade → asset prices.

Economic interest:

- ▶ Organization of market with two functions.

Question

Does collateral function complement funding function?

- ▶ What happens to eq'm funding absent collateral demand?
- ▶ Does this effect vary over time or in crises?
- ▶ Implications for regulation and policy?

What we do

Our focus: **distribution of collateral demand across firms.**

1. Transaction data of repo against UK gov bonds with firm ids.
→ Heterogeneity in repo rates across firms.
2. Equilibrium model of repo.
→ Effect of heterogeneous collateral demand across firms.
3. Structurally estimate model.
→ Infer & interrogate firm-time-asset collateral demand.
→ Counterfactual: remove collateral demand.

What we find

Does collateral function complement liquidity function?

No! Volumes and gains to trade higher absent collateral demand.

- ▶ Joint distribution of funding and collateral needs across firms.
- ▶ Firms that need funding are also those that value collateral.

Empirical literature on repo

Duffie (1996); Gorton and Metrick (2012); Copeland, Martin & Walker (2014); Krishnamurthy, Nagel & Orlov (2014); Mancini, Rinaldo & Wrampelmeyer (2016); Boissel, Derrien, Ors & Thesmar (2017); D'Amico, Fan & Kitsul (2018); Rinaldo, Schaffner & Tsatsaronis (2019); Hüser, Lepore & Veraart (2021); Eisenschmidt, Ma & Zhang (2022); Ballensiefen, Rinaldo & Winterberg (2023); Huber (2023).

Contribution

1. Structural measurement of collateral demand.
2. Distribution in XS and TS.
3. Equilibrium effects.
4. Negative effect on repo market functioning.

Empirical literature on repo: Specialness

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Empirical literature on repo: Structural estimation

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Table of Contents

Data and facts

Model

Estimation

Results

Counterfactual

Conclusion

Empirical Facts

BoE transaction data on \approx universe of repo trading against UK government collateral (gilts) from 2017-23.

Facts on collateral demand:

1. Underlying asset matters for hedge funds, not MMFs.
2. Most repo rates below risk-free rate.
3. Hedge funds charge lower rates to lend.
4. Rates higher when collateral is interchangeable.

Background facts:

- ▶ Market power, exogenous networks, interdealer trade, etc.

Rate Variation: Hedge Fund vs MMF Lending

Table reports R^2 in regression of repo rates on FE for firm type.

Fixed effects	Hedge fund	MMF
Week-Maturity	0.50	0.31
Week-Maturity-Borrower	0.56	0.98
Week-Maturity-Lender	0.62	0.42
Week-Maturity-Asset	0.94	0.73

What about:

1. q ?
2. confounding factors?
3. quantification?
4. counterfactuals?

→ **model**

Table of Contents

Data and facts

Model

Estimation

Results

Counterfactual

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Model: Setup

Assets & Agents

- ▶ \mathcal{A} assets, indexed by a : exchange cash for collateral.
- ▶ Return to funding for agent $i \sim N(\nu_i, 1)$.
- ▶ Return to collateral for agent $i \sim N(\eta_i^a, \sigma)$.
- ▶ Mean-var preferences with risk aversion κ .

Trading structure

- ▶ N_d dealers and N_c customers on fixed network \mathbf{G}^a .
 - ▶ Firm k has set \mathcal{N}_k^a as neighbours.
 - ▶ No customer-customer links.
1. Competitive interdealer market indexed by D .
 2. Dealer-customer trade, where dealers have market power.

Model: Setup

Trading

- ▶ q_{ij}^a borrowing by i from j against a .
- ▶ $Q_i^a = \sum_{j \in \mathcal{N}_i^a} q_{ij}^a$ total net borrowing by i against a .
- ▶ $Q_i = \sum_a Q_i^a$ total net borrowing by i .
- ▶ r_{ij}^a interest rate.
- ▶ ϵ_{im}^a non-pecuniary, relationship-specific benefits.

Payoff to firm i

$$\underbrace{\nu_i Q_i}_{\text{Funding}} - \underbrace{\frac{\kappa}{2} Q_i^2 - \sum_a \eta_i^a Q_i^a - \sum_a \frac{\kappa}{2} \sigma (Q_i^a)^2}_{\text{Collateral demand}} - \underbrace{\sum_a \sum_{m \in \mathcal{N}_i^a} q_{im}^a (r_{im}^a + \epsilon_{im}^a)}_{\text{Transaction terms}}$$

First order condition

Customer j , with respect to quantity q_{ij}^a :

$$\underbrace{-\nu_j + \kappa Q_j}_{-j\text{'s MB from cash}} \quad \underbrace{+\eta_j^a + \kappa\sigma Q_j^a}_{j\text{'s MB from collateral}} \quad + r_{ij}^a = 0$$

Dealer i , with respect to quantity q_{ij}^a :

$$\underbrace{\nu_i - \kappa Q_i}_{i\text{'s MB from cash}} \quad \underbrace{-(\eta_i^a + \kappa\sigma Q_i^a)}_{-i\text{'s MB from collateral}} \quad \underbrace{-\kappa \sum_l q_{ij}^l - \kappa\sigma q_{ij}^a - \epsilon_{ij}^a - r_{ij}^a}_{\text{Price effect}} = 0$$

Equilibrium

Solution:

- ▶ Linear FOCs where network link exists, given \mathbf{G} .

Equilibrium quantity q_{ij}^a depends on:

- ▶ Relative counterparty characteristics: v_i, v_j and η_i^a, η_j^a .
- ▶ Network: counterparties' counterparties' characteristics, etc.

Effect of collateral demand on gains to trade ($\eta_i^a = 0, \forall i$):

- ▶ Correlation between funding and collateral demand across i .
- ▶ Therefore an empirical question. Example

Table of Contents

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Model

Estimation

Results

Counterfactual

Conclusion

Estimation: Setting

Task is to recover as flexibly as possible

- ▶ funding demand ν_{it} ;
- ▶ collateral demand η_{it}^a ;
- ▶ risk σ ; and
- ▶ risk aversion κ ;

from

- ▶ observed quantities q_{ijt}^a ; and
- ▶ observed rates r_{ijt}^a .

Estimation: Overview

Model: Dealer i FOC with respect to q_{ijt}^a :

$$r_{ijt}^a = \underbrace{\nu_{it} - \kappa Q_{it}}_{i\text{'s MB from cash}} - \underbrace{(\eta_{it}^a + \kappa\sigma Q_{it}^a)}_{i\text{'s MB from collateral}} - \underbrace{\kappa \sum_l q_{ijlt}^l - \kappa\sigma q_{ijt}^a - \epsilon_{ijt}^a}_{\text{Price effect}}$$

Two step estimation:

1. Infer (κ, σ) from variation across j , within $i - t$.
2. Given these estimates, infer (ν_{it}, η_{it}^a) from variation across a .

Challenges:

- ▶ Simultaneity: Gilt prices and trading patterns by firm as IV.
- ▶ Level identification: $\eta_{it}^a = 0$ when a is "general collateral".

Details

Table of Contents

Data and facts

Model

Estimation

Results

Counterfactual

Conclusion

Results

Variation across firms:

1. Variation across type: banks and HF have high η .
2. Positive correlation across firms between η and ν .

Variation across time:

3. Funding demand tracks central bank rate.
4. Level and dispersion in collateral demand track volatility.

Implication:

- ▶ Collateral demand bad for funding, particularly in stress?

Hedging

Correlation

Vol

Variation in Funding & Collateral Demand

Most variation across firms, not across assets:

Fixed Effects	Funding demand	Collateral demand
Time t	0.96	0.07
Firm i	0.14	0.49
Asset a		0.05
Firm-Asset ia		0.58
Firm-Time it		0.85
Asset-Time at		0.19

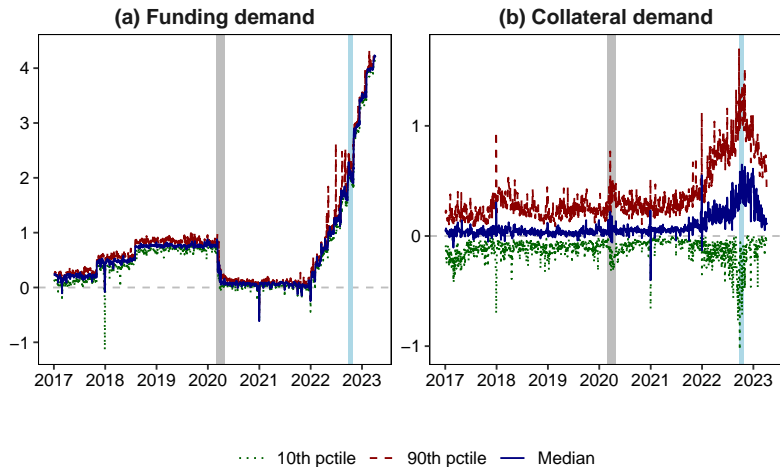
Variation across firm types

	Funding demand ν_{it}	Collateral demand η_{it}^a
	(1)	(2)
Bank	0.68*** (0.007)	0.13*** (0.0007)
Dealer	0.81*** (0.006)	0.23*** (0.0004)
Fund	0.84*** (0.005)	0.07*** (0.001)
Hedge Fund	0.70*** (0.004)	0.11*** (0.0007)
MMF	0.61*** (0.01)	0.05*** (0.003)
Other	0.77*** (0.008)	0.13*** (0.002)
PFLDI	0.71*** (0.006)	-0.08*** (0.001)
R ²	0.005	0.05
Observations	167,037	1,490,509

Correlation between funding and collateral demand

	Collateral demand η_{it}^a		
	(1)	(2)	(3)
Funding demand ν_{it}	0.20*** (0.0003)	0.95*** (0.001)	0.12*** (0.02)
R ²	0.22	0.74	0.57
Observations	1,563,051	1,563,051	1,563,051
Day FEs		Yes	
Firm FEs			Yes

Variation over time



Results

Variation across firms:

1. Variation across type: banks and HF have high η .
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Variation across time:

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Table of Contents

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Model

Estimation

Results

Counterfactual

Conclusion

Counterfactual: Removing Collateral Demand

Removing collateral demand:

- ▶ Set $\eta_{it}^a = 0$ for all a, i, t .
- ▶ Collateral equally useful for everyone only as insurance.

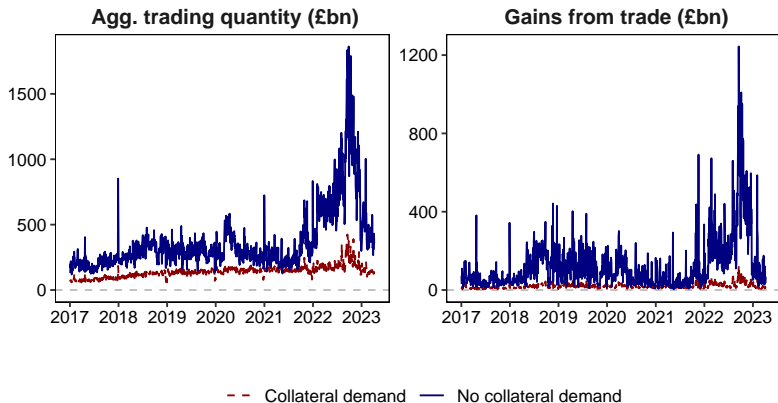
Effect, relative to baseline:

- ▶ Volumes and gains to trade higher, particularly in stress.

Extension, wrt correlation:

- ▶ Rearrange η_{it}^a across i to reverse correlation.
- ▶ Undertake same counterfactual removing collateral demand.
- ▶ Effect reversed: this is about correlation.

Counterfactual: Quantities & GTT



Role of Correlation

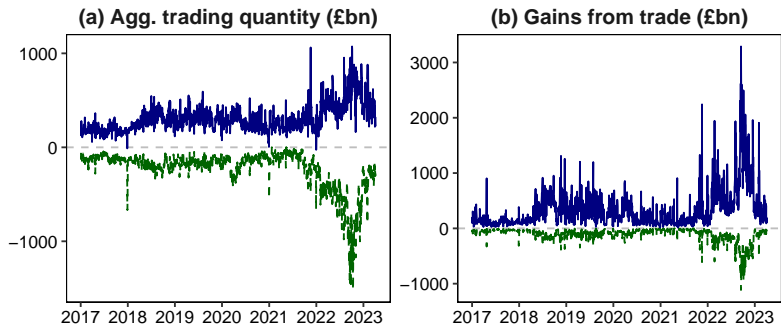


Table of Contents

Data and facts

Model

Estimation

Results

Counterfactual

Conclusion

Regulation

Problem: banks cannot simultaneously manage risk and funding.

- ▶ Banks need to be long on bonds to fund themselves...
- ▶ ... when they want to reduce inventory risk.

Implications for regulation/policy?

- ▶ Uncovered short-selling.
- ▶ Central bank repo accepting other collateral.
- ▶ Central bank collateral swap facilities.
- ▶ Monetary policy.

Conclusion

- ▶ Collateral demand is a key driver of repo outcomes.
- ▶ Effect depends on joint distribution with funding demand.
- ▶ Finding: dual repo functions do not always combine well.

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- ▶ Effect depends on joint distribution with funding demand.
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Thank you!
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Annexes

Background facts

Trade details:

- ▶ Mostly short maturity.
- ▶ Fully or over collateralized, no default.

Trade structure:

- ▶ Network sparse & broadly fixed. [Details](#)
- ▶ Dealers earn a spread. [Dealer spreads](#)
- ▶ D-D trade mostly on platforms, D-C trade OTC.

Firm types:

- ▶ MMFs uniquely lend, do not use collateral. [Details](#)
- ▶ Hedge funds borrow & lend, and may use to short.
- ▶ Different firms borrow against different gilts. [Wallet variation](#)

Net lending by sector

	Trade Share (%)	Daily net lending (%)	Daily net lending (£bn)
Dealer	66.1	-3.8	-4.6
Bank	11.7	-31.4	-7.5
Hedge Fund	10.3	-0.2	-0.4
Fund	4.2	62.5	5.2
MMF	2.9	97.4	6.2
PFLDI	2.8	18.9	0.9
Other	2.0	0.6	0.5

Additional facts

1. Fewer than 2% of counterparty pairs have non-zero trade in the whole sample.
2. Over 95% of transactions after January 2022 onwards were between traders who had traded together before January 2022.

[Back](#)

Repo rate variation

Fixed effects	R-squared
<i>Deal characteristics</i>	
Week	0.37
Week-Asset	0.86
Week-Maturity	0.42
Week-Asset-Maturity	0.90
<i>Trader characteristics</i>	
Week-Borrower	0.51
Week-Lender	0.45
Week-Borrower-Lender	0.59

Rate variation

Dealer spreads

	Repo rate (%)		
	(1)	(2)	(3)
Dealer lending	0.155*** (0.007)	0.149*** (0.002)	0.092*** (0.0006)
R ²	0.23	0.35	0.81
Observations	1,003,270	1,003,270	1,003,270
Week FEs	Yes		
Week-Dealer FEs		Yes	
Week-Dealer-Asset FEs			Yes

Repo Rates & Collateralization Type

		Repo rate (%)		
	(1)	(2)	(3)	(4)
General Collateral	0.09*** (0.006)	0.09*** (0.01)	0.09*** (0.003)	0.10*** (0.004)
R ²	0.30	0.20	0.55	0.43
Observations	6,095,617	6,095,617	6,095,617	6,095,617
Week FEs	Yes			
Borrower-Lender FEs		Yes		
Borrower-Week FEs			Yes	
Lender-Week FEs				Yes

Back

Rates for hedge funds vs MMFs

		Repo rate (%)		
	(1)	(2)	(3)	(4)
Lender: Hedge fund	-0.06*** (0.006)	-0.08*** (0.003)	-0.003*** (0.001)	-0.002** (0.001)
R ²	0.38	0.58	0.94	0.97
Observations	371,649	371,649	371,649	371,649
Week FEs	Yes			
Borrower-Week FEs		Yes		
Borrower-Asset-Week FEs			Yes	
Asset-Mat-Borr-Week FEs				Yes

Back

Model: Simplified example

One dealer i , one customer j , one asset:

- ▶ $\Delta\nu \equiv \nu_i - \nu_j$, $\Delta\eta \equiv \eta_i - \eta_j$.
- ▶ Equilibrium net borrowing by i :

$$q_{ij} = \frac{\Delta\nu - \Delta\eta}{3\kappa(1 + \sigma)}$$

- ▶ Equilibrium trading volume:

$$|q_{ij}| = \frac{|\Delta\nu - \Delta\eta|}{3\kappa(1 + \sigma)}$$

- ▶ Gains to trade:

$$GTT = \frac{2(\Delta\nu - \Delta\eta)^2}{9\kappa(1 + \sigma)}$$

Model: Simplified example

One dealer i , one customer j , one asset:

- ▶ $\Delta\nu \equiv \nu_i - \nu_j$, $\Delta\eta \equiv \rho\bar{\eta}\Delta\nu$.
 - ▶ $\rho \in [-1, 1]$: correlation btw liquidity and collateral demand.
 - ▶ $\bar{\eta} \in [0, 1]$: magnitude of collateral demand.
- ▶ Effect of collateral demand on GTT depends on correlation ρ :

$$\frac{dGTT}{d\bar{\eta}} \begin{cases} > 0, & \text{if } \rho < 0 \\ < 0, & \text{otherwise} \end{cases}$$

- ▶ Effect of collateral demand therefore an empirical question.

Back

Estimation: Step 1

Estimating equation:

$$r_{ijt}^a = \delta_{it}^a - \left[\kappa \sum_l q_{ijt}^l + \kappa \sigma q_{ijt}^a \right] \mathbb{1}_{ij} + \epsilon_{ijt}^a$$

where $\mathbb{1}_{ij} = 1$ if i has market power wrt j .

Identification:

- ▶ Challenge: standard joint determination of q and r .
- ▶ Different j trade different a (exogenous "wallet").
- ▶ Change in price of gilt a exogenous to ϵ_{ijt}^a .
- ▶ Shift-share IV: lag wallet shares, interact with price.

Estimation

Details

Estimation: Step 2

Model:

$$\delta_{it}^a = \nu_{it} - \kappa Q_{it} - \eta_{it}^a - \kappa\sigma \sum_m q_{imt}^a$$

Second step estimation:

$$\hat{\delta}_{it}^a + \hat{\kappa}\hat{\sigma} \sum_m q_{imt}^a + \hat{\kappa}Q_{it} = \nu_{it} - \eta_{it}^a$$

- ▶ Decompose network-adjusted average interest rates for i .
- ▶ Level identification from following assumption:

$$\eta_{it}^{GC} = 0 \quad \forall i, t$$

Instruments: Details

Instruments:

$$z_{1,jt} = \sum_{a \in \omega_j} s_{jt}^a \times \text{price}_t^a$$

$$z_{2,jt}^a = z_{1,jt} - s_{jt}^a \times \text{price}_t^a$$

First stage:

$$q_{ijt}^a = \alpha_{it}^a + \beta_1 z_{1,jt} + \beta_2 z_{2,jt}^a + e_{ijt}^a$$
$$\sum_l q_{ijt}^l = \alpha_{it}^a + \beta_3 z_{1,jt} + \beta_4 z_{2,jt}^a + e_{ijt}^a$$

Second stage:

$$r_{ijt}^a = \delta_{it}^a - \left[\kappa \sum_l q_{ijt}^l + \kappa \sigma q_{ijt}^a \right] \mathbf{1}_{ij} + \epsilon_{ijt}^a$$

Back

Estimates: risk & risk aversion

	Repo rate r_{ijt}^a (%)	
	OLS (1)	2SLS (2)
$\sum_l q_{ijt}^l$	-0.01*** (0.0009)	-0.02*** (0.002)
q_{ijt}^a	-0.12*** (0.002)	-0.18*** (0.003)
Wald (1st stage), $\sum_l q_{ijt}^l$		6,377.2
Wald (1st stage), q_{ijt}^a		2,170.8
R ²	0.996	0.997
Within R ²	0.027	0.037
Observations	599,384	527,295
Firm-asset-day FEs	Yes	Yes
Firm-counterparty FEs	Yes	Yes

First Stage

	q_{ijt}^a OLS (1)	$\sum_l q_{ijt}^l$ 2SLS (2)
$z_{1,jt}$	-0.0114*** (0.0002)	-0.0072*** (0.0002)
$z_{2,jt}^a$	0.0116*** (0.0002)	0.0009*** (0.0002)
R ²	0.80069	0.86838
F-test	535.18	878.98
Observations	527,295	527,295
Firm-asset-week FEs	Yes	Yes
Firm-counterparty FEs	Yes	Yes

Back

Collateral Demand & Asset Prices

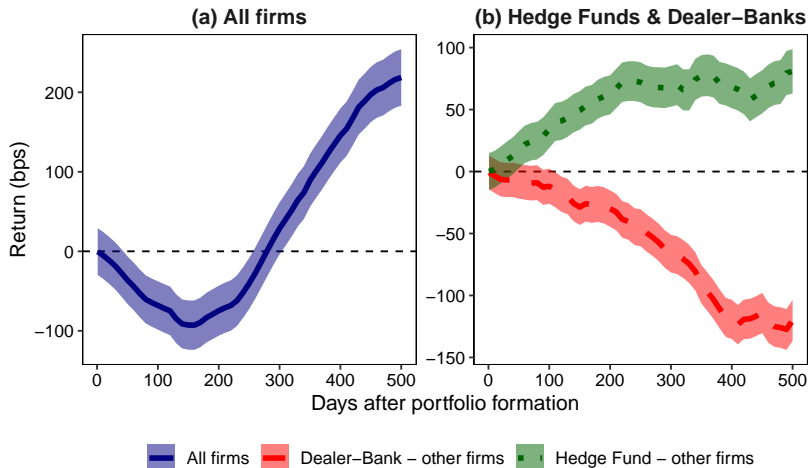
Questions:

- ▶ Why do banks have collateral demand?
- ▶ Does collateral demand predict future bond prices?
- ▶ Is collateral demand about hedging or speculation?

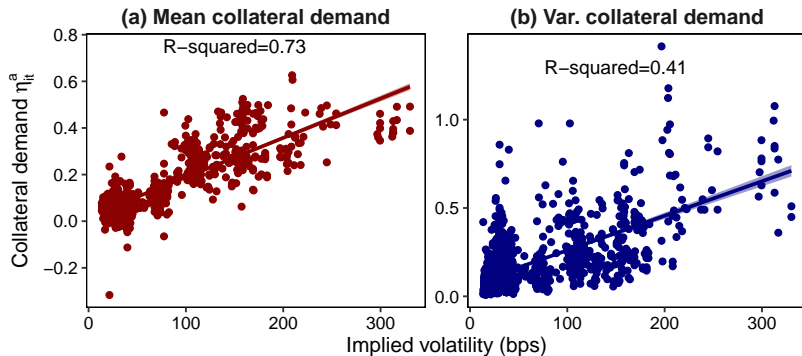
Approach:

- ▶ Go short (long) on bonds with high (low) collateral demand.

3. Collateral Demand & Asset Prices



Volatility & Collateral Demand



Back

Sector heterogeneity

	Trade Share (%)	Daily net lending (%)	Daily net lending (£bn)
Dealer	66.1	-3.8	-4.6
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Week-Lender	0.45
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Rate variation by firm type

Fixed effects	Hedge fund	MMF
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Week-Maturity-Borrower	0.56	0.98
Week-Maturity-Lender	0.62	0.42
Week-Maturity-Asset	0.94	0.73

Rates for general collateral

		Repo rate (%)		
	(1)	(2)	(3)	(4)
General Collateral	0.09*** (0.006)	0.09*** (0.01)	0.09*** (0.003)	0.10*** (0.004)
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Borrower-Week FEs			Yes	
Lender-Week FEs				Yes

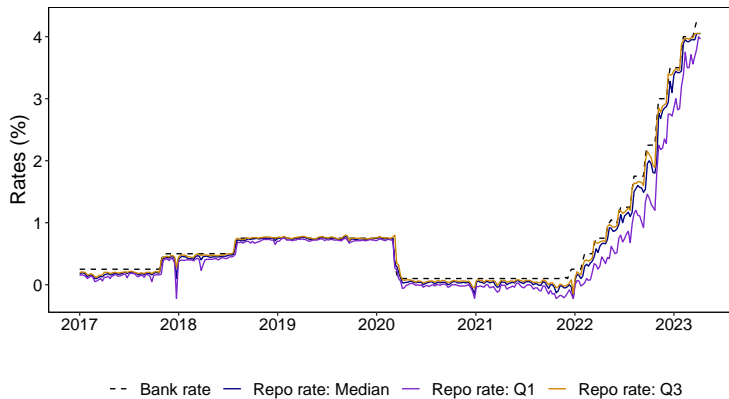
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Week-Dealer FEs		Yes	
Week-Dealer-Asset FEs			Yes

Rates through time on dealer repo lending



Regression Results

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Implied volatility

